

(i) Printed Pages: 3

Roll No. ....

(ii) Questions : 8

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Exam. Code : 

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**B.A./B.Sc. (General) 1<sup>st</sup> Semester**

**(1129)**

**MATHEMATICS**

**Paper—II**

**(Calculus—I)**

**Time Allowed : Three Hours]**

**[Maximum Marks : 30**

**Note :—** Attempt *five* questions in all, selecting at least *two* questions from each of the Unit I and II.

**UNIT—I**

I. (a) Between any two distinct real numbers, there is always an irrational number, and therefore, infinitely many irrational numbers.

(b) If  $|x - 5| < 1$ , then prove that :  $\frac{x^2 - 2x - 1}{x - 3} \in \left(\frac{17}{3}, 9\right)$ .  
3,3

II. (a) Prove that  $\lim_{x \rightarrow c} \frac{1}{x - c}$  does not exist.

(b) Find l.u.b and g.l.b., if exists, for the set :

$\left\{ \frac{2+x}{1-x} : x > 0, x \neq 1 \right\}$  3,3

**0044/FF-8077**

**1**

**[Turn over**

III. (a) If a function  $f$  is continuous at  $x = c$  and  $f(c) \neq 0$ , then prove that there exists a neighbourhood of  $c$ , where  $f(x)$  and  $f(c)$  has the same sign.

(b) Show that the function  $f$  defined by :

$$f(x) = \begin{cases} [x-3] + [3-x], & x \neq 3 \\ 0 & , x = 3 \end{cases}$$

is discontinuous at  $x = 3$ .

3,3

IV. (a) Evaluate :

$$\lim_{x \rightarrow 1} \frac{x^x - x}{x - 1 - \log x}$$

(b) Find the values of  $a$ ,  $b$  and  $c$ , if

$$\lim_{x \rightarrow 0} \frac{(a + b \cos x)x - c \sin x}{x^5} = 1$$

3,3

### UNIT—II

V. (a) State and prove Cauchy's mean value theorem.

(b) Use mean value theorem to prove that :

$$\frac{\pi}{6} + \frac{2x-1}{\sqrt{3}} \leq \sin^{-1} x \leq \frac{\pi}{6} + \frac{2x-1}{2\sqrt{1-x^2}} \text{ for } \frac{1}{2} \leq x < 1. \quad 3,3$$

VI. (a) Differentiate w.r.t  $x$

$$e^{\tanh^{-1}\left(\frac{2x}{1-x^2}\right)} + \sinh^{-1}(\operatorname{sech} x) \cdot$$

(b) Use Taylor's theorem to express :

$$f(x) = 2 + x^2 - 3x^5 + 7x^6 \text{ in powers of } (x - 1).$$

3,3

VII. (a) Show that  $\coth^{-1}x = \frac{1}{2} \log\left(\frac{x+1}{x-1}\right)$  for  $|x| > 1$  and hence find its derivative.

(b) Use Maclaurin's theorem to prove

$$\sin^2 x = x^2 - \frac{x^4}{3} + \frac{2}{45}x^6 - \dots \quad 3,3$$

VIII. (a) If  $\sqrt{x} + \sqrt{y} = \sqrt{a}$ , show that  $\frac{d^2y}{dx^2} = \frac{1}{2a}$  at  $x = a$ .

(b) If  $x = \cos\left(\frac{1}{m} \log y\right)$ , prove that :

$$(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} - (n^2 + m^2)y_n = 0. \quad 3,3$$

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